



## **EEEN 462 – ANALOGUE COMMUNICATION**

### **AMPLITUDE MODULATION (AM) STUDY GUIDE**

#### **1. INTRODUCTION**

Amplitude Modulation (AM) is an analogue modulation technique where the **amplitude** of a high-frequency carrier wave is varied **in proportion** to the instantaneous amplitude of a lower-frequency message (modulating) signal. It's fundamental in radio broadcasting (AM radio) and forms the basis for understanding many other modulation schemes.

##### **1. Signals & Systems:**

- Continuous-Time (CT) vs. Discrete-Time (DT) signals.
- Periodic vs. Aperiodic signals.
- Basic signal operations (scaling, shifting, addition, multiplication).
- Concept of frequency (Hz).

##### **2. Fourier Analysis:**

- Understanding the frequency domain representation of a signal (Fourier Transform - FT).
- Concept of bandwidth (BW) - the range of frequencies a signal occupies.
- Spectrum of a pure sinusoid (impulse at  $\pm f_c$ ).
- Spectrum of a baseband message signal (occupying 0 to  $f_m$  Hz).

##### **3. Need for Modulation:**

- Antenna size proportional to wavelength ( $\lambda = c/f$ ). Low-frequency signals require impractical antenna sizes.
- Frequency Division Multiplexing (FDM): Multiple signals transmitted simultaneously over the same medium using different carrier frequencies.
- Ease of radiation for higher frequencies.
- Overcoming noise/interference limitations at baseband.

#### **2. AM: MATHEMATICAL REPRESENTATION**

##### **1. The Carrier Wave: $c(t) = A_c * \cos(2\pi f_c t + \phi_c)$**

- $A_c$ : Carrier Amplitude (Constant in unmodulated state)
- $f_c$ : Carrier Frequency ( $\gg$  message frequency  $f_m$ )
- $\phi_c$ : Carrier Phase (Often assumed 0 for simplicity)

## 2. The Message Signal: $m(t)$

- Represents the information (e.g., audio, data).
- Bandwidth = B Hz (Occupies 0 to B Hz).
- Maximum Amplitude =  $m_p$ .

## 3. Standard AM (DSB-FC - Double Sideband Full Carrier):

### ○ Time Domain Expression:

$$s_{AM}(t) = A_c * [1 + \mu * m_n(t)] * \cos(2\pi f_c t)$$

- $s_{AM}(t)$ : Modulated AM signal.
- $m_n(t) = m(t) / m_p$ : Normalized message signal ( $-1 \leq m_n(t) \leq 1$ ).
- $\mu = k * m_p$ : **Modulation Index** (Critical Parameter!)
  - $k$ : Sensitivity constant of the modulator ( $V^{-1}$ ).
  - $0 \leq \mu \leq 1$  required to avoid distortion (Overmodulation).
- **Envelope**: The term  $A_c * [1 + \mu * m_n(t)]$  is the **envelope** of the AM signal. The message  $m_n(t)$  *must* lie within this envelope for distortion-free demodulation.

## 3. MODULATION INDEX (M)

### 1. Definition: $\mu = (A_{max} - A_{min}) / (A_{max} + A_{min})$

- $A_{max}$ : Maximum amplitude of the modulated wave envelope.
- $A_{min}$ : Minimum amplitude of the modulated wave envelope.

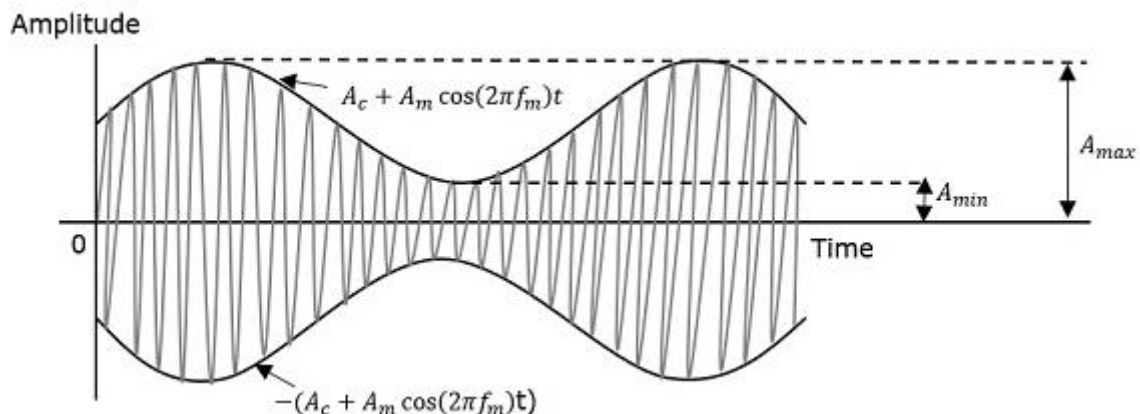


Figure 1. AM Modulation Index

### 2. Significance:

- $\mu = 0$ : No modulation (Carrier only).
- $0 < \mu < 1$ : Under-modulation (Correct operation).
- $\mu = 1$ : 100% modulation (Envelope touches zero at minima).
- $\mu > 1$ : Over-modulation (Envelope crosses zero, causing severe distortion - "Envelope Inversion").

3. **Percentage Modulation:** % Modulation =  $\mu * 100\%$

#### 4. FREQUENCY DOMAIN ANALYSIS (SPECTRUM)

1. **Assume Simple Message:**  $m(t) = A_m * \cos(2\pi f_m t)$  (Single tone for clarity).

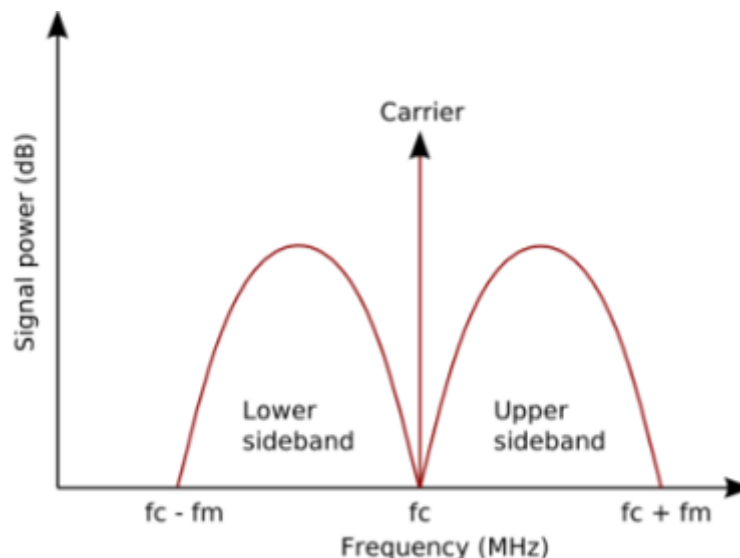
2. **AM Signal:**  $s_{AM}(t) = A_c [1 + \mu \cos(2\pi f_m t)] \cos(2\pi f_c t)$

3. **Trigonometric Expansion:**

$$s_{AM}(t) = A_c \cos(2\pi f_c t) + (A_c \mu / 2) \cos(2\pi(f_c + f_m)t) + (A_c \mu / 2) \cos(2\pi(f_c - f_m)t)$$

4. **Spectrum Components:**

- **Carrier:** Amplitude =  $A_c$ , Frequency =  $f_c$ .
- **Upper Sideband (USB):** Amplitude =  $A_c \mu / 2$ , Frequency =  $f_c + f_m$ .
- **Lower Sideband (LSB):** Amplitude =  $A_c \mu / 2$ , Frequency =  $f_c - f_m$ .



**Figure 2.** Spectrum Components in AM signal

5. **General Message Spectrum:**

- Carrier remains at  $f_c$ .
- USB: Exact replica of the *message spectrum* shifted up to frequencies  $f_c$  to  $f_c + B$ .
- LSB: Exact replica of the *message spectrum* shifted down to frequencies  $f_c - B$  to  $f_c$ .
- **Bandwidth (BW):**  $BW_{AM} = 2 * B$  (Twice the message bandwidth).

#### 5. POWER DISTRIBUTION

1. **Total Transmitted Power ( $P_t$ ):**

$$P_t = P_c + P_{usb} + P_{lsb}$$

2. **Carrier Power ( $P_c$ ):**

$$P_c = (A_c^2) / 2 \frac{A_c^2}{2} \text{ (Average power of } A_c \cos(\omega_c t) \text{ across } 1\Omega \text{ resistor)}$$

3. **Sideband Power (Each):**

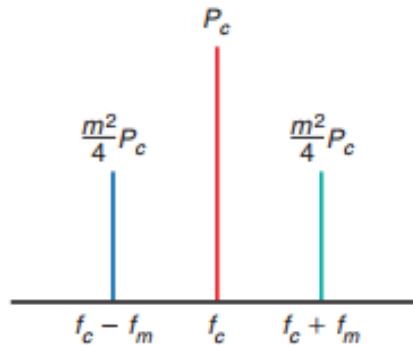
$$P_{usb} = P_{lsb} = (A_c \mu / 2)^2 / 2 = (A_c^2 \mu^2) / 8$$

4. **Total Sideband Power ( $P_{sb}$ ):**

$$P_{sb} = P_{usb} + P_{lsb} = (A_c^2 \mu^2) / 4$$

5. **Total Power ( $P_t$ ):**

$$P_t = P_c + P_{sb} = (A_c^2 / 2) + (A_c^2 \mu^2 / 4) = (A_c^2 / 2) * [1 + (\mu^2 / 2)]$$



**Figure 3.** Power distribution in AM signal

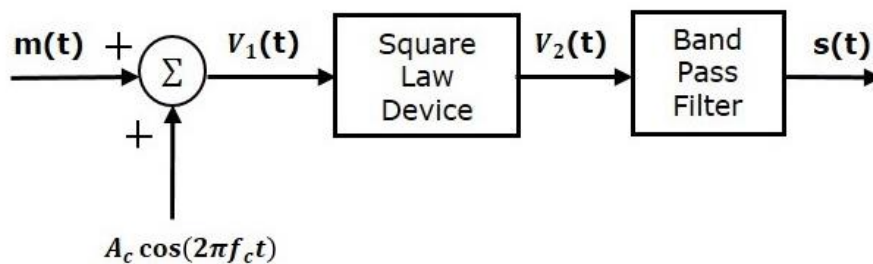
6. **Power Efficiency ( $\eta_{AM}$ ):**

$$\eta_{AM} = (P_{sb} / P_t) * 100\% = (\mu^2 / (2 + \mu^2)) * 100\%$$

- **Maximum Efficiency:** At  $\mu=1$ ,  $\eta_{max} = (1 / (2 + 1)) * 100\% = 33.3\%$ . **Most power ( $\geq 66.7\%$ ) is wasted in the carrier!**

## 6. GENERATION METHODS (CONCEPTUAL)

1. **Square Law Modulator:** Uses the non-linear (square-law) region of a device (e.g., diode, transistor).  $s_{AM} \approx k_1 * c(t) + k_2 * [c(t) + m(t)]^2$ .



**Figure 4.** AM square law Modulator

2. **Switching Modulator:** Uses a device (e.g., diode, FET) acting as a switch controlled by the carrier. Effective multiplication.

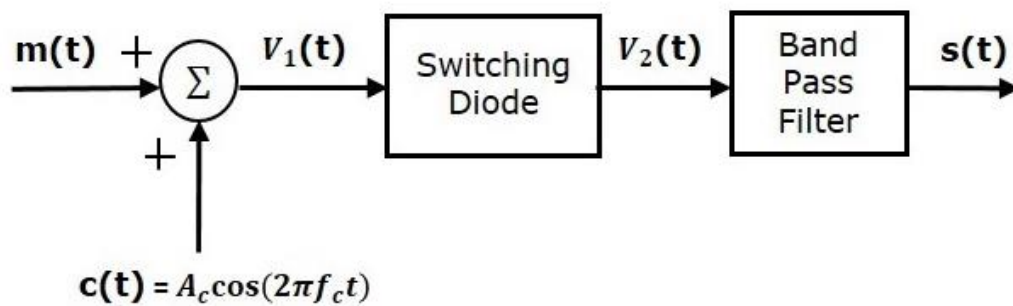


Figure 5. Switching AM modulator

3. **Balanced Modulator (for DSB-SC)** consists of two identical AM modulators. These two modulators are arranged in a balanced configuration in order to suppress the carrier signal as shown below.

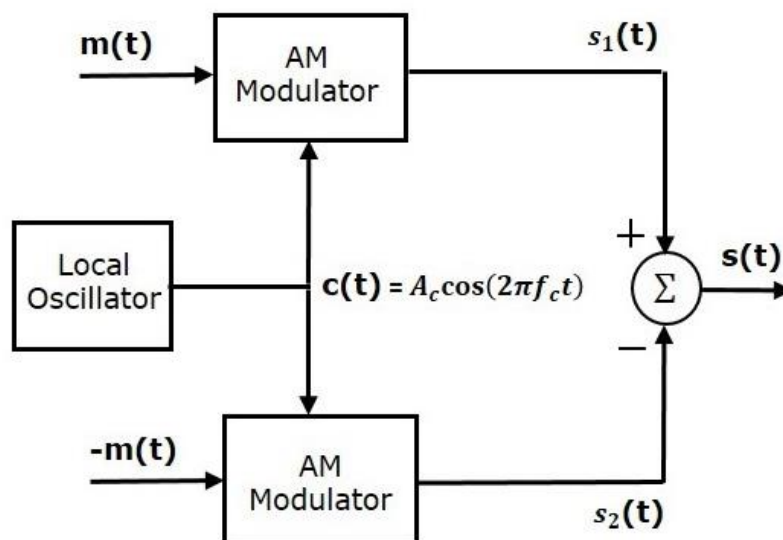


Figure 5. Balanced AM Modulator

## 7. DEMODULATION (DETECTION) METHODS

### 1. Envelope Detector:

- **Principle:** Extract the envelope of the AM wave.
- **Circuit:** Simple diode (half-wave rectifier) + RC low-pass filter.
- **Pros:** Very simple, cheap, used in most AM radios.
- **Cons:** Requires  $\mu \leq 1$  (no overmodulation); Performance degrades significantly with noise; Cannot demodulate DSB-SC/SSB.

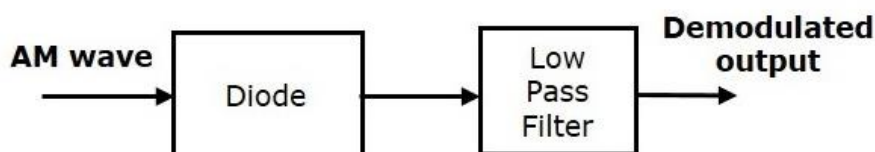


Figure 6. Envelope detector

## 2. Synchronous Detection (Coherent Detection):

- **Principle:** Multiply the received signal  $r(t) = s_{AM}(t)$  by a *local oscillator* signal  $\cos(2\pi f_c t)$  synchronized in frequency and phase with the original carrier.
- **Process:**  $r(t) * \cos(\omega_c t) = s_{AM}(t) * \cos(\omega_c t) = \dots = (A_c/2)[1 + \mu m_n(t)] + (A_c/2)[1 + \mu m_n(t)] \cos(2\omega_c t)$
- **Low-Pass Filtering:** Removes the high-frequency  $2\omega_c$  component, leaving  $(A_c/2)[1 + \mu m_n(t)]$ . DC blocking recovers  $m_n(t)$ .
- **Pros:** Can demodulate DSB-SC and SSB; More resilient to noise than envelope detector (in theory).
- **Cons:** Requires generating a *coherent* local carrier ( $f_c$  and  $\phi_c$  match precisely) - complex and expensive; Carrier recovery needed for suppressed carrier schemes.

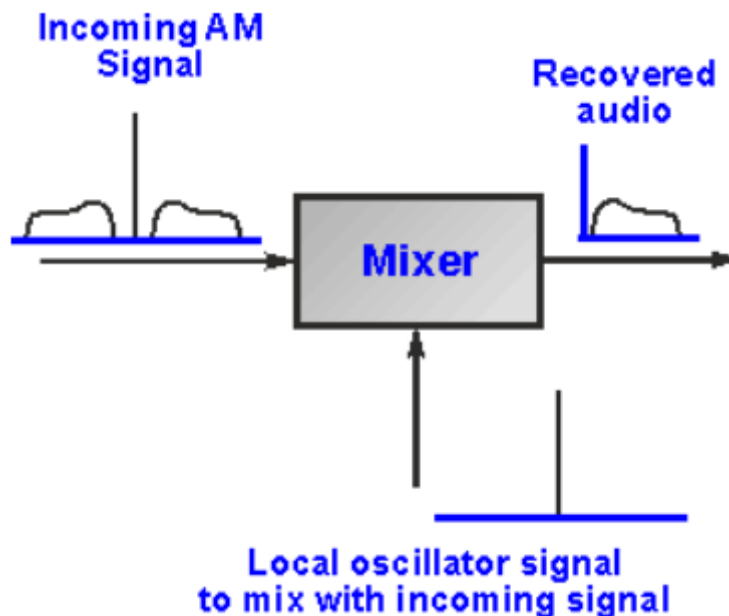


Figure 7. Synchronous AM demodulator

## 8. DRAWBACKS OF STANDARD AM (DSB-FC)

1. **Low Power Efficiency:**  $\geq 66.7\%$  of power wasted in the carrier (esp. when  $\mu < 1$ ).
2. **Inefficient Spectrum Usage:** Bandwidth is  $2B$ , while the information is duplicated in both sidebands.
3. **Susceptibility to Noise:** Noise affects the amplitude directly, corrupting the information. Envelope detectors are particularly noise-sensitive.

## 9. IMPROVED AM VARIANTS (CONCEPTUAL)

### 1. Double Sideband Suppressed Carrier (DSB-SC):

- $s_{DSB-SC}(t) = A_c m(t) \cos(\omega_c t)$

- **Spectrum:** Carrier absent; Only USB & LSB present.
- **Bandwidth:** 2B (Same as AM).
- **Efficiency:** 100% of power is in sidebands (theoretically more efficient).
- **Demodulation:** Requires synchronous detection (complex).

## 2. Single Sideband (SSB):

- $s_{SSB}(t) \approx A_c m(t) \cos(\omega_c t) \mp A_c \hat{m}(t) \sin(\omega_c t)$  (USB/LSB)
- **Spectrum:** Carrier absent; *Either* USB or LSB present.
- **Bandwidth:** B (Half of AM/DSB-SC).
- **Efficiency:** 100% of power in one sideband (most efficient spectrum & power usage).
- **Generation/Demodulation:** More complex (requires filters or phasing methods; demodulation requires synchronous detection).

3. **Vestigial Sideband (VSB):** A compromise between DSB and SSB, used in analog TV transmission. One full sideband + a "vestige" of the other.

## 10. KEY APPLICATIONS

1. **AM Radio Broadcasting (535-1705 kHz):** Standard DSB-FC. Simplicity of receivers (envelope detectors) was crucial historically.
2. **Aircraft VHF Communications (118-136 MHz):** Sometimes uses AM for voice.
3. **Video Transmission in Analog TV:** Used VSB to save bandwidth.
4. **QAM (Quadrature Amplitude Modulation):** Digital modulation scheme building on DSB-SC principles (uses I/Q channels).

## 11. IMPORTANT CONSIDERATIONS & TERMINOLOGY

- **Overmodulation:** Causes distortion and "envelope inversion". Avoid  $\mu > 1$ .
- **Sideband Suppression:** Techniques to remove one sideband (SSB) or the carrier (DSB-SC).
- **Coherent vs. Non-Coherent Detection:** Envelope detector is non-coherent; Synchronous detector is coherent.
- **Selective Fading:** Affects different spectral components differently. Can cause distortion in AM, especially if carrier fades.

## 12. STUDY TIPS

1. **Master the Math:** Derive the time-domain expression and spectrum for a single-tone AM signal.
2. **Visualize Spectra:** Sketch spectra for carrier, message, and AM signal.
3. **Understand Modulation Index ( $\mu$ ):** Calculate it, understand its impact on waveform, spectrum, and power.

4. **Know the Trade-offs:** Why use DSB-FC despite its inefficiency? (Receiver simplicity). Why use SSB? (Bandwidth/power efficiency).
5. **Compare Techniques:** Make a table comparing DSB-FC, DSB-SC, SSB, VSB (Carrier? Sidebands? BW? Efficiency? Demod Complexity? Apps).
6. **Practice Power Calculations:** Be able to derive and calculate  $P_c$ ,  $P_{sb}$ ,  $P_t$ ,  $\eta_{AM}$ .
7. **Know Demodulation Principles:** How envelope detector and synchronous detector work, their pros/cons.

## **12. LAB COMPONENT**

1. Generate AM signals using a function generator and oscilloscope. Measure modulation index.
2. Write a MATLAB function to simulate amplitude modulation.
3. Build a simple diode envelope detector circuit. Observe output vs. input.
4. Use a spectrum analyzer to view AM, DSB-SC, and SSB spectra.